Progression in Number and Place Value

|  | Year 3 | Year 4 | Year 5 |
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Progression in Addition and Subtraction

|  | Year 3 | Year 4 | Year 5 | Year 6 |
| :---: | :---: | :---: | :---: | :---: |
|  | Add and subtract numbers mentally including: <br> - a three-digit numbers and ones <br> - a three-digit numbers and tens <br> - a three-digit numbers and hundreds |  | Add and subtract numbers mentally with increasingly large numbers | Perform mental calculations, including with mixed operations and large numbers |
|  | Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction | Add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate | Add and subtract whole numbers with more than 4 digits including using formal written methods (columnar addition and subtraction) |  |
|  | Estimate the answer to a calculation and use inverse operations to check answers | Estimate and use inverse operations to check answers to a calculation | Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy | Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy |
| 年 | Solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction | Solve addition and subtraction twostep problems in contexts, deciding which operations and methods to use and why | Solve addition and subtraction multistep problems in contexts, deciding which operations and methods to use and why | Solve addition and subtraction multistep problems in contexts, deciding which operations and methods to use and why |
|  |  |  |  | Solve problems involving addition, subtraction, multiplication and division |
| 年 |  |  |  | Use their knowledge of the order of operations to carry out calculations involving the four operations |

Progression in Multiplication and Division

|  | Year 3 | Year 4 | Year 5 | Year 6 |
| :---: | :---: | :---: | :---: | :---: |
|  | Recall and use multiplication and division facts for the 3,4 and 8 multiplication tables | Recall multiplication and division facts for multiplication tables up to $12 \times 12$ | Multiply and divide whole numbers and those involving decimals by 10,100 and 1000 |  |
|  | Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit | Use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1 ; dividing by 1 ; multiplying together three numbers | Multiply and divide numbers mentally drawing upon known facts | Perform mental calculations, including with mixed operations and large numbers |
|  | numbers, using mental and progressing to formal written methods | Multiply two-digit and three-digit numbers by a one-digit number using formal written layout | Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers | Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication |
| $\frac{. \bar{n}}{\frac{.0}{2}}$ |  |  | Divide numbers up to 4 digits by a onedigit number using the formal written method of short division and interpret remainders appropriately for the context | Divide numbers up to 4 digits by a twodigit number using the formal written method of short division where appropriate, interpreting remainders according to the context |
|  |  |  |  | Divide numbers up to 4 digits by a twodigit whole number using the formal written method of long division and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context |


|  |  | Recognise and use factor pairs and commutativity in mental calculations | Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers | Identify common factors, common multiples and prime numbers |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | Know and use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers |  |
|  |  |  | Establish whether a number up to 100 is prime and recall prime numbers up to 19 |  |
|  |  |  | Recognise and use square numbers and cube numbers, and the notation for squared ( ${ }^{2}$ ) and cubed ( ${ }^{3}$ ) |  |
| $\begin{aligned} & \text { ow } \\ & \frac{0}{0} \\ & \text { E} \\ & \text { E} \\ & \text { 운 } \end{aligned}$ | Solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which $n$ objects are connected to m objects | Solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to mobjects | Solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes | Solve problems involving addition, subtraction, multiplication and division |
|  |  |  | Solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign |  |
|  |  |  | Solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates |  |
| 年 |  |  |  | Use their knowledge of the order of operations to carry out calculations involving the four operations |
|  |  |  |  | Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy |

Progression in Fractions, Decimals and Percentages


|  | Compare and order unit fractions, and fractions with the same denominators |  | Compare and order fractions whose denominators are all multiples of the same number | Compare and order fractions, including fractions $>1$ |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | Recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements $>1$ as a mixed number (for example $2 / 5+4 / 5=6 / 5=1$ 1/5) |  |
|  | Record $1 / 10$ as $0.1,3 / 10$ as 0.3 etc. | Recognise and write decimal equivalents of any number of tenths or hundredths | Read and write decimal numbers as fractions (for example $0.71=71 / 100$ ) | Associate a fraction with division and calculate decimal fraction equivalents for a simple fraction (for example 0.375 $=3 / 8$ ) |
|  |  | Recognise and write decimal equivalents to $1 / 41 / 23 / 4$ | Solve problems which require knowing percentage and decimal equivalents of $1 / 2,1 / 4,1 / 5,2 / 5,4 / 5$ and those with a denominator of a multiple of 10 or 25 | Recall and use equivalences between simple fractions, decimals and percentages, including in different contexts |
|  |  | Round decimals with one decimal place to the nearest whole number | Round decimals with two decimal places to the nearest whole number and to one decimal place |  |
|  |  | Find the effect of dividing a one- or twodigit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths | Read, write, order and compare numbers with up to three decimal places | Identify the value of each digit to three decimal places and multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places |
|  |  | Compare numbers with the same number of decimal places up to two decimal places |  |  |
|  |  |  | Recognise the per cent symbol (\%) and understand that per cent relates to "number of parts per hundred", and write percentages as a fraction with denominator 100 , and as a decimal | Solve problems involving the calculation of percentages (for example, of measures such as $15 \%$ of 360 ) and the use of percentages for comparison (Ratio and Proportion) |


|  |  |  |  | Multiply one-digit numbers with up to two decimal places by whole numbers <br> Use written division methods in cases where the answer has up to two decimal places |
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|  |  |  |  |  |
| $\begin{aligned} & \text { 틍 } \\ & \text { 음 } \\ & \text { 응 } \\ & \end{aligned}$ | Solve fraction problems | Solve simple measure and money problems involving fractions and decimals to two decimal places | Solve problems involving number up to three decimal places | Solve problems which require answers to be rounded to specified degrees of accuracy |

## Progression in Measurement

|  | Year 3 | Year 4 | Year 5 |
| :--- | :--- | :--- | :--- | :--- |
|  | Measure, compare, add and subtract: <br> lengths (m/cm/mm); mass $(\mathrm{kg} / \mathrm{g}) ;$ <br> volume/capacity $(\mathrm{l} / \mathrm{ml})$ | Estimate, compare and calculate <br> different measure, including money in <br> pounds and pence |  |


|  |  |  | Estimate volume (for example, using 1 $\mathrm{cm}^{3}$ blocks to build cuboids, including cubes) and capacity (for example using water) | Calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres ( $\mathrm{cm}^{3}$ ) and cubic metres $\left(\mathrm{m}^{3}\right)$, and extending to other units (for examples $\mathrm{mm}^{3}$ and $\mathrm{km}^{3}$ ) |
| :---: | :---: | :---: | :---: | :---: |
| $\stackrel{\text { E, }}{\underline{\text { E }}}$ | Tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks <br> Estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes and hours; use vocabulary such as o'clock, a.m./p.m., morning, afternoon, noon and midnight | Read, write and convert time between analogue and digital 12 and 24-hour clocks | Solve problems involving converting between units of time (Link- statistics- timetables) |  |
|  | Know the number of seconds in a minute and the number of days in each month, year and leap year Compare durations of events (for example, to calculate the time taken by particular events or tasks) | Solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days |  |  |
|  |  |  | Use all four operations to solve problems involving measure (for example, length, mass, volume, money) using decimal notation including scaling | Solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate |

Progression in Geometry: Properties of Shapes

|  | Year 3 | Year 4 | Year 5 | Year 6 |
| :---: | :---: | :---: | :---: | :---: |
|  | Identify horizontal and vertical lines and pairs of perpendicular and parallel lines | Compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes | Identify 3-D shapes, including cubes and other cuboids, from 2-D representations | Compare and classify geometric shapes based on their properties and sizes |
|  |  |  | Distinguish between regular and irregular polygons based on reasoning about equal sides and angles | Illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius |
|  | Draw 2-D shapes and make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them |  |  | Draw 2-D shapes using given dimensions and angles |
|  |  |  |  | Recognise, describe and build simple 3D shapes, including making nets |
|  | Recognise angles as a property of shape or a description of a turn | Identify acute and obtuse angles and compare and order angles up to two right angles by size | Know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles | Recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles |
|  | Identify right angles, recognise that two right angles make a half-turn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle |  | Draw given angles, and measure them in degrees ( ${ }^{\circ}$ ) |  |
|  |  |  | Identify: <br> - angles at a point and one whole turn (total $360^{\circ}$ ) <br> - angles at a point on a straight line and $1 / 2$ a turn (total $180^{\circ}$ ) <br> - other multiples of $90^{\circ}$ | Find unknown angles in any triangles, quadrilaterals, and regular polygons |
|  |  |  | Use the properties of rectangles to deduce related facts and find missing lengths and angles |  |
|  |  | Identify lines of symmetry in 2-D shapes presented in different orientations |  |  |


|  | Complete a simple symmetric figure <br> with respect to a specific line of <br> symmetry |  |
| :--- | :--- | :--- | :--- | :--- |

Progression in Geometry: Position and Direction

|  |  | Year 3 | Year 4 |  |
| :--- | :--- | :--- | :--- | :--- |

Progression in Statistics

|  | Year 3 | Year 4 | Year 5 | Year 6 |
| :---: | :---: | :---: | :---: | :---: |
|  | Interpret and present data using bar charts, pictograms and tables | Interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs | Complete, read and interpret information in tables, including timetables | Interpret and construct pie charts and line graphs and use these to solve problems |
|  | Solve one-step and two-step questions (for example, 'How many more?' and 'How many fewer?') using information presented in scaled bar charts and pictograms and tables | Solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs | Solve comparison, sum and difference problems using information presented in a line graph | Calculate and interpret the mean as an average |

## Progression in Ratio and Proportion

|  | Year 3 | Year 4 | Year 5 | Year 6 |
| :---: | :---: | :---: | :---: | :---: |
|  | Solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which $n$ objects are connected to m objects (Link: Multiplication and Division) | Solve problems involving multiplying and adding, including integer scaling problems and harder correspondence problems such as n objects are | Solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates <br> (Link: Multiplication and Division) | Solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts |
|  |  | connected to m objects <br> (Link: Multiplication and Division) |  | Solve problems involving unequal sharing and grouping using knowledge of fractions and multiples |
| 咢 |  |  |  | Solve problems involving similar shapes where the scale factor is known or can be found |

Progression in Algebra

|  | Year 3 | Year 4 | Year 5 | Year 6 |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | Non-Statutory: <br> Recognise and describe linear number sequences including those involving fractions and decimals, and find the term-to-term rule in words | Generate and describe linear number sequences |
|  | Estimate the answer to a calculation and use inverse operations to check answers (Link: Addition and Subtraction) | Estimate and use inverse operations to check answers to a calculation (Link: Addition and Subtraction) | Non-Statutory: <br> Use multiplication and division as inverses <br> (Link: Multiplication and Division) | Express missing number problems algebraically |
|  |  |  |  | Use simple formulae |
|  |  |  |  | Find pairs of numbers that satisfy an equation with two unknowns |
|  |  |  |  | Enumerate possibilities of combinations of two variables |

